Motility control as a (self-)organization pathway for motile particles

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LMU: 2019 Arnold Sommerfeld School on the Physics of Life

Equilibrium Statistical Mechanics

- Large thermostat with chaotic dynamics
- Exchange energy with the system
- Drives the system towards thermal equilibrium

	System	
Thermostat		

 \longrightarrow Boltzmann distribution $P_{\text{stat}}(\mathcal{C}) \propto \exp[-\beta E(\mathcal{C})]$

→ Time-reversal symmetry in steady-state (detailed-balance)

Non-equilib. phys. is like non-elephant biology



no steady state

no Boltzmann weight

no time-reversal symmetry

Some examples

Glasses



Boundary driven



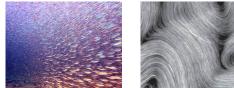
Active matter



Identify coherent subclasses and say something smart/useful about them!

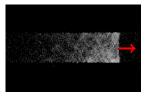
Active matter

Mechanical drive at the microscopic level ->> Strongly out of equilibrium ->> Fundamentally new physics



Fish shoals

Motility assays

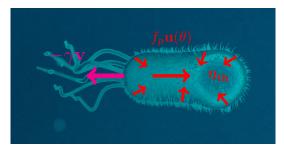


Colloidal Rollers

- New dynamical phenomenology
- Biological relevance
- Active Soft Materials

- Motility-induced phase separation
- No guiding principles
- Active pressure

Active matter



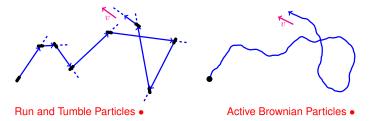
$0 = m\dot{v} = -V'_{\text{ext}}(x) - \gamma v + \sqrt{2\gamma kT}\eta + f_p \mathbf{u}(\theta)\tilde{\eta} + f_p \mathbf{u}(\theta) + f_p f_p f_p f_p$

- Colloid in a fluid at equilibrium: Fluctuation-Dissipation theorem $D = kT/\gamma$ Active matter: \rightarrow No FDT: system driven out of equilibrium
 - \longrightarrow Dissipation: mean (drag) force from the fluid $\propto \gamma$
 - \rightarrow Injection of energy: fluctuating force from the fluid $\propto \gamma kT$
 - \longrightarrow Injection of energy: self-propulsion force $f_p \mathbf{u}(\theta)$

Self-organization in & out of equilibrium

- Equilibrium physics
 - → Time-reversal symmetry in steady-state
 - -> Replace dynamical studies by ensemble approach
 - → Intuition based on Boltzman weight
- Example: Liquid-gas phase transition
 - -> Passive Brownian particles with attractive interactions
 - -> Entropy vs Energy : disorder vs cohesion
 - \rightarrow Lowering T: transition from gas to liquid (with coexistence)
- Outside equilibrium
 - → No generic formula for steady-state distribution
 - -> Little basis upon which to build intuition
 - → Few guiding principles for self-assembly

Motility-control as a self-organization principle



- Self-propelled particles with propelling speed v
- Diverse reorientation mechanisms (ABPs, RTPs, AOUPs, etc.)
- Generic: properties of $v \longrightarrow$ Control steady states
 - I. Non-interacting particles with spatially varying speed $v(\mathbf{r})$
- II. Quorum-sensing: density-dependent speed $v(\rho)$
- III. Application to bacterial pattern formation
- IV. Multi-species systems
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